

## Parameterization of a Two-Phase Sheet Flow Model and Application to Nearshore Morphology

Steve Elgar and Tian-Jian Hsu  
Applied Ocean Physics and Engineering,  
Woods Hole Oceanographic Institution, MS #11,  
Woods Hole, MA 02543  
Phone: 508-289-2654, Fax: 508-457-2194,  
Email: thsu@whoi.edu (Hsu), elgar@whoi.edu (Elgar)  
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Daniel M. Hanes  
U.S. Geological Survey Pacific Science Center  
1156 High Street, Santa Cruz, CA 95064

### Objectives

The overall objective is to develop and test with laboratory and field observations a model that predicts sediment transport and morphological change in the nearshore for a range of wave conditions and sediment characteristics. The specific objectives of this project were to

1. parameterize the wave-induced bottom stress and sediment transport rate using a two-phase sheet flow model,
2. couple the sediment transport model with a time-domain Boussinesq hydrodynamic model to predict beach profile evolution, and
3. improve the two-phase sheet flow model by comparing its predictions with laboratory and field observations of sediment transport.

### Work Completed

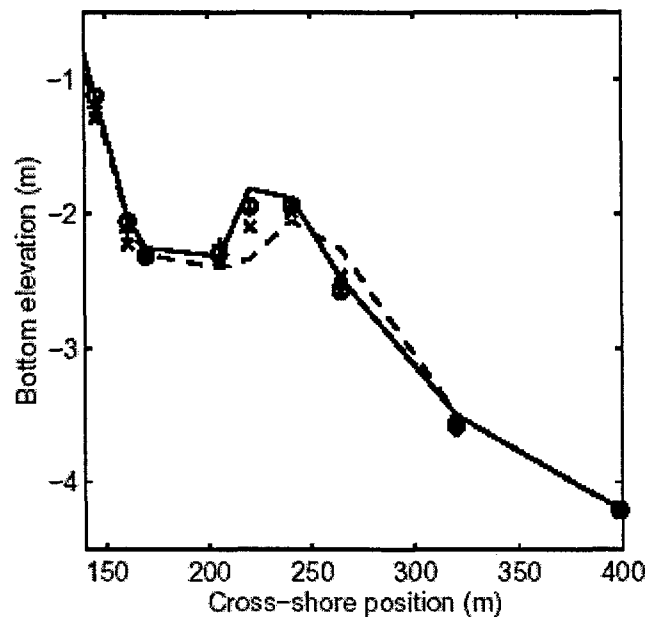
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A small-scale two-phase model [Hsu *et al.* 2004] that concurrently calculates bedload and suspended load transport processes was used to parameterize sediment transport. An earlier study [Hsu and Hanes 2004] considered simple wave shapes and suggested that most transport may be in-phase with bottom stress and hence the transport rate can be parameterized by a power law. In the beginning of this project, realistic wave forcing time series measured during the Duck94 [Gallagher *et al.* 1998] and SwashX [Raubenheimer 2002] field experiments were utilized to drive the two-phase model and a diluted suspended load model [Hsu and Liu 2004]. The validity of the power law approach was confirmed for typical sand grain sizes ( $d > \sim 0.2\text{mm}$ ) and wave periods ( $T > 5\text{sec}$ ). The limitation of the power law approach due to the effect of breaking wave turbulence also was studied using field data. The power law must be accompanied with a prediction of bottom stress to obtain the transport rate. Similar to that predicted by a discrete element model [Drake and Calantoni 2001], model results tested here with realistic wave forcing also suggest that under strong pitched-forward sea-swell waves, the

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effect of the boundary layer phase-lag on bottom stress is important. Detailed findings were summarized in a paper [Hsu and Raubenheimer, in press] to appear in Continental Shelf Research.

According to these small-scale analyses, several simplified (computationally efficient) approaches that effectively parameterize the effects of the boundary layer and the concentrated region of transport were developed to predict beach profile evolution. When driven by the wave forcing measured during the Duck94 experiment [Gallagher *et al.*, 1998], these simplified approaches were shown to be capable of predicting an observed 5-day onshore sandbar migration event with different degrees of accuracy (see figure 1 for details). Detailed results and findings are summarized in a paper submitted for publication [Hsu, Elgar, and Guza, submitted].



**Figure 1: Bottom elevation (i.e., depth relative to mean sea level) versus cross-shore position observed September 22 (dashed curve) and September 27 (solid curve) 1994. Symbols are model predictions of the September 27 profile initialized with the September 22 profile and driven with near-bottom wave-orbital (i.e., demeaned) velocities observed between 1900 September 22 and 2200 September 27. Crosses (x) are the quasi-steady model with a wave friction factor  $f_w = 0.01$ , plusses (+) are the second-order single-phase flow model with a mixing-length closure (roughness,  $K_s = 14d$ ), and circles are the second-order model with  $k-\epsilon$  closure ( $K_s = 25d$ ). The quasi-steady model has moderate model skill (0.34), whereas the second-order model with mixing length closure has higher skill (0.57). The highest skill (0.69, circles) is obtained using  $k-\epsilon$  closure in the second-order model.**

These simplified approaches for sediment transport are further incorporated into a Boussinesq wave model, FUNWAVE. Given the measured offshore wave conditions and initial bathymetry, the Boussinesq model is able to reproduce both the observed surfzone hydrodynamics and beach profile evolution during an onshore sandbar migration event.

Preliminary results were published in a conference proceeding [Long, Hsu, and Kirby, 2005]. More detailed results, including erosional conditions are currently in preparation for publication.

Due to the strong undertow current, accurate prediction of beach erosion requires an effective bottom stress parameterization for combined wave-current flow. We developed a standard wave-current boundary layer model (similar to Mellor [2002]) that simultaneously resolves the wave and current boundary layers using the Reynolds-Averaged Navier-Stokes (RANS) equation. This type of numerical model captures the nonlinear wave-current interactions and provides accurate bottom stress. However, it is computationally time-consuming to couple these wave-current boundary models directly with wave models for a predictive tool of beach morphology. Under a combined wave-current forcing, the computational requirement for the RANS boundary layer model is significant because the horizontal pressure gradient (energy slope) required to achieve the desired current velocity is not known *a priori* [Grant and Madsen 1979] and an iteration procedure is needed. However, given a time history of near-bed flow velocity, it is efficient to calculate only the bottom stress induced by pure oscillatory forcing or pure current forcing (without wave-current interaction). Here, we proposed an efficient phase-resolving bottom stress parameterization for such wave-current interactions. The performance of the new parameterization was tested extensively with random wave forcing (CROSSTEX, Duck94, and SwashX). Detailed numerical model development, validations, and parameterization for wave-current bottom stress are summarized in a paper submitted for publication [Hsu, submitted].

Progress also has been made to extend the two-phase model to simulate transport of finer sand. Preliminary comparisons of model simulations with U-tube data measured by Dohmen-Janssen *et al.* [2002] and O'Donoghue and Wright [2004] suggest that the refined closure for turbulence-sediment interactions calibrated by the DNS results [Squires and Eaton, 1994] is promising. A manuscript summarizing these results is currently in preparation.

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Long, W., Hsu, T.-J., and Kirby, J. T. 2005. Modeling cross-shore sediment transport processes with a time domain Boussinesq model, *Proceedings 29<sup>th</sup> International Conference on Coastal Engineering*, Vol. 2, 1874-1886.

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Hsu, T.-J., Elgar, S. and Guza, R. T. A wave-resolving approach to modeling onshore sandbar migration, submitted.

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